1. Consider a standard 30-year, fixed-rate mortgage with monthly payments and interest rate of $4.5 \%$, with $\$ 300,000$ principal.
(a) (10 points) What is the equivalent annual yield on this mortgage?
(b) ( $\mathbf{2 5}$ points) We can evaluate this annuity using two perpetuities. Explain what these 2 perpetuities are, how we use them to obtain the relevant Annuity Factor for this mortgage, and show the Annuity Factor for this mortgage.
(c) ( $\mathbf{1 5}$ points) What is the size of the monthly payment of this mortgage?
(d) ( 25 points) Show the first two months of the mortgage amortization table-i.e., how much of the first two payments goes to interest, and how much to principal.
2. ( $\mathbf{1 5}$ points) Your parents are considering retiring. They would like to purchase an annuity that provides a monthly cash flow of $\$ 5,000$ for the next 25 years. The banks that they have spoken with have told them that the current rate on such products is $3 \%$. How much will such an annuity cost?
3. ( $\mathbf{1 0}$ points) Suppose that a perpetual government bond which pays $\$ 300$ every 6 months (the next payment is in exactly six months) sells for $\$ 9,090.91$. What is the bond equivalent (i.e., semi-annually compounded) yield on this perpetual government bond?
